

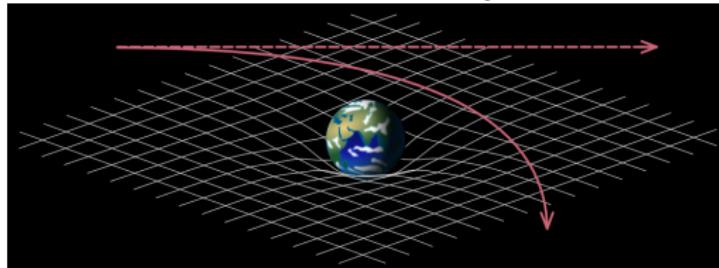
# **Cosmology with weak gravitational lensing**

Chieh-An Lin (Linc)

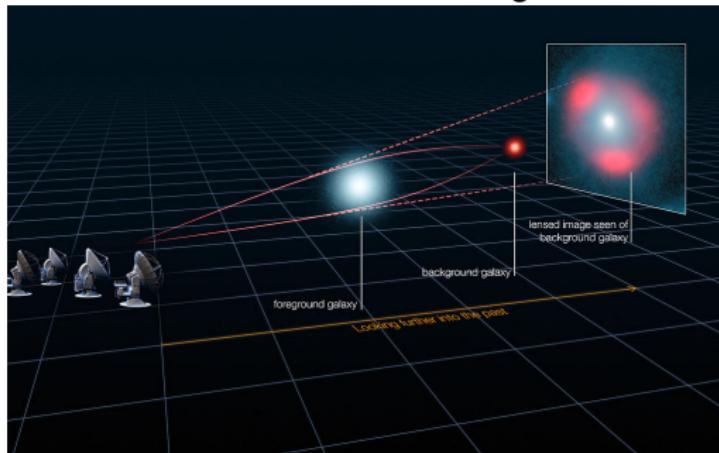
June 18<sup>th</sup>, 2020

National Taiwan Normal University

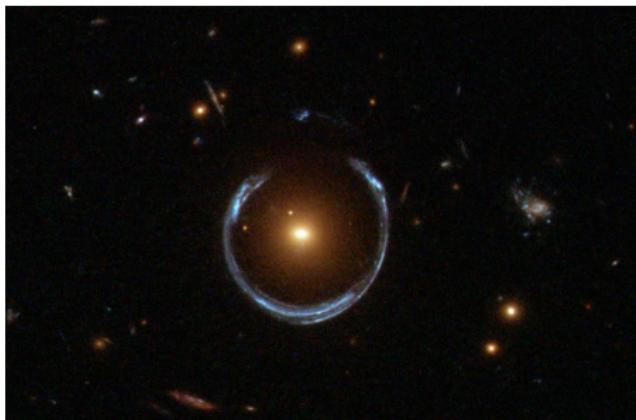
## General relativity



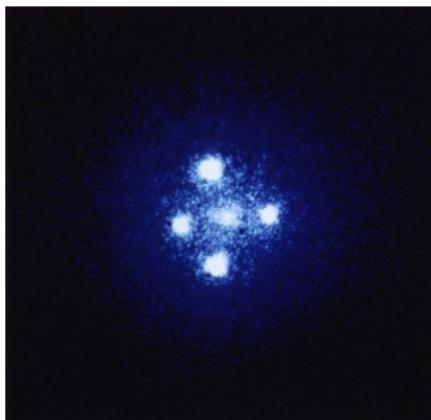
## Gravitational lensing



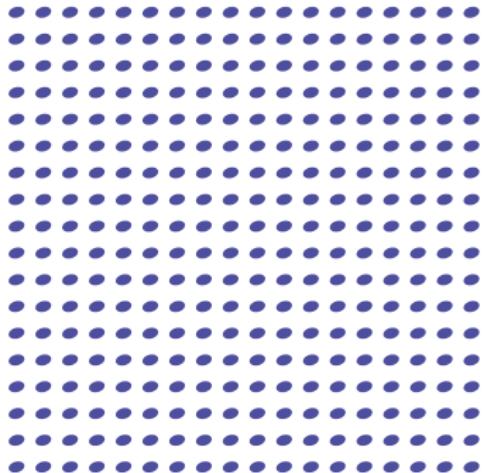
Source: ALMA



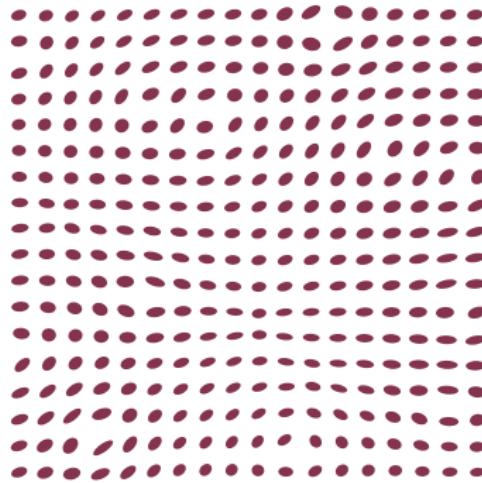
Strong lenses



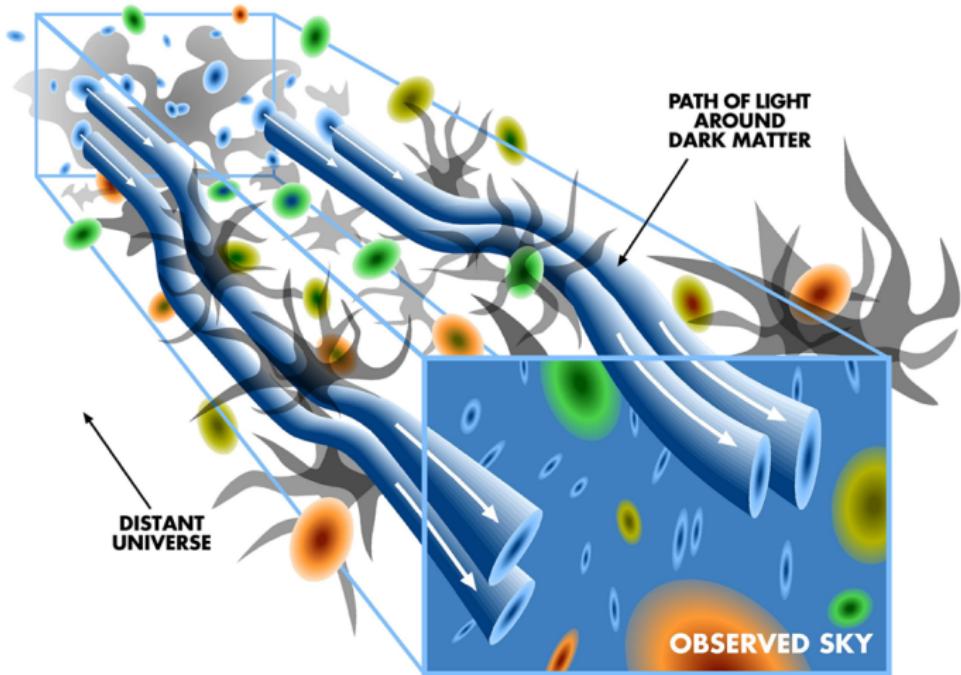
Source: SDSS, HST



Unlensed sources

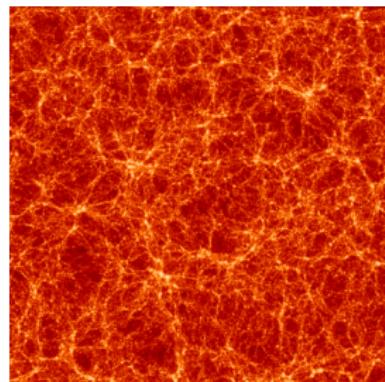


Weak lensing

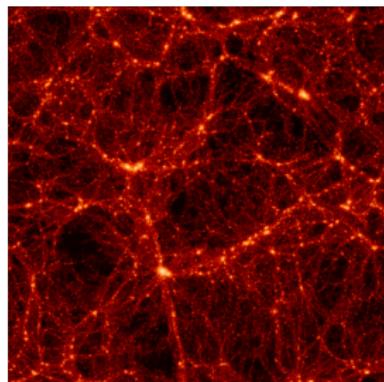


Source: LSST

## LSS from different models

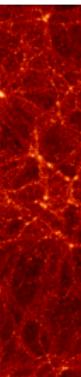


SCDM

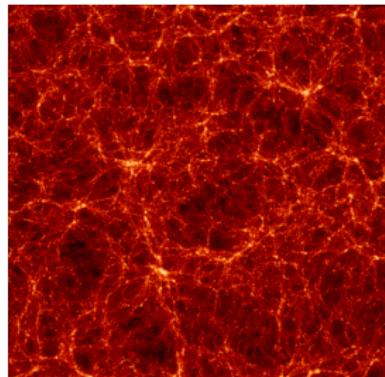


OCDM

$\Lambda$ CDM



$\tau$ CDM



Abundance  $\Omega_m$   
Fluctuation  $\sigma_8$

(Credit: J. Colberg, Virgo)

# Outline

Scientific motivations What to measure

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Theoretical basis How to measure

---

Observational challenges What do we really measure

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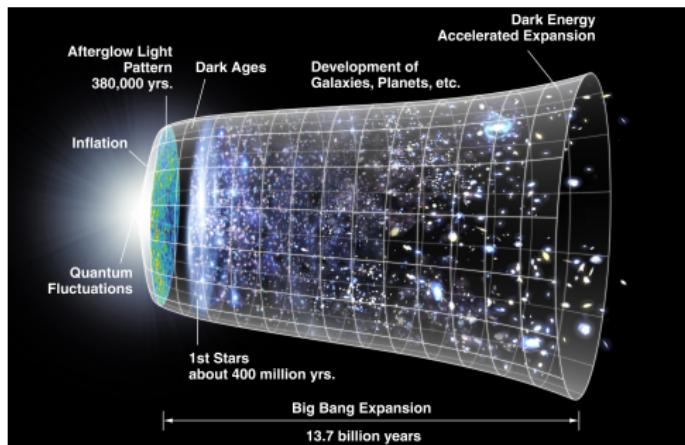
State of the art What have been measured

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Future perspectives What will be measured

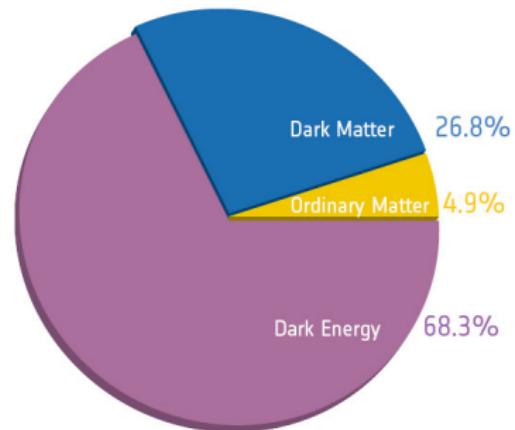
## **Scientific motivations**

## Cosmic timeline



(Source: NASA)

## Cosmic recipe

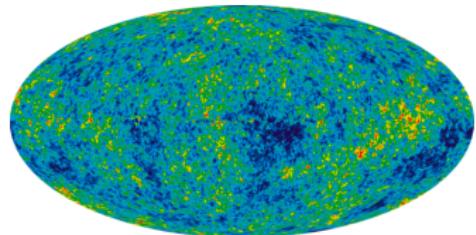


(Source: ESA)

“ $\Lambda$ CDM model”

## Cosmological probes

Cosmic microwave background



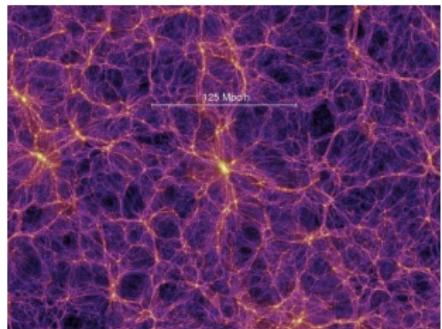
(Source: WMAP)

Type Ia supernovae



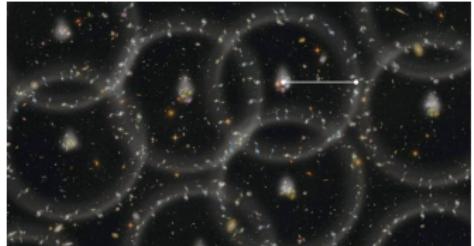
(Source: NASA)

Large-scale structures

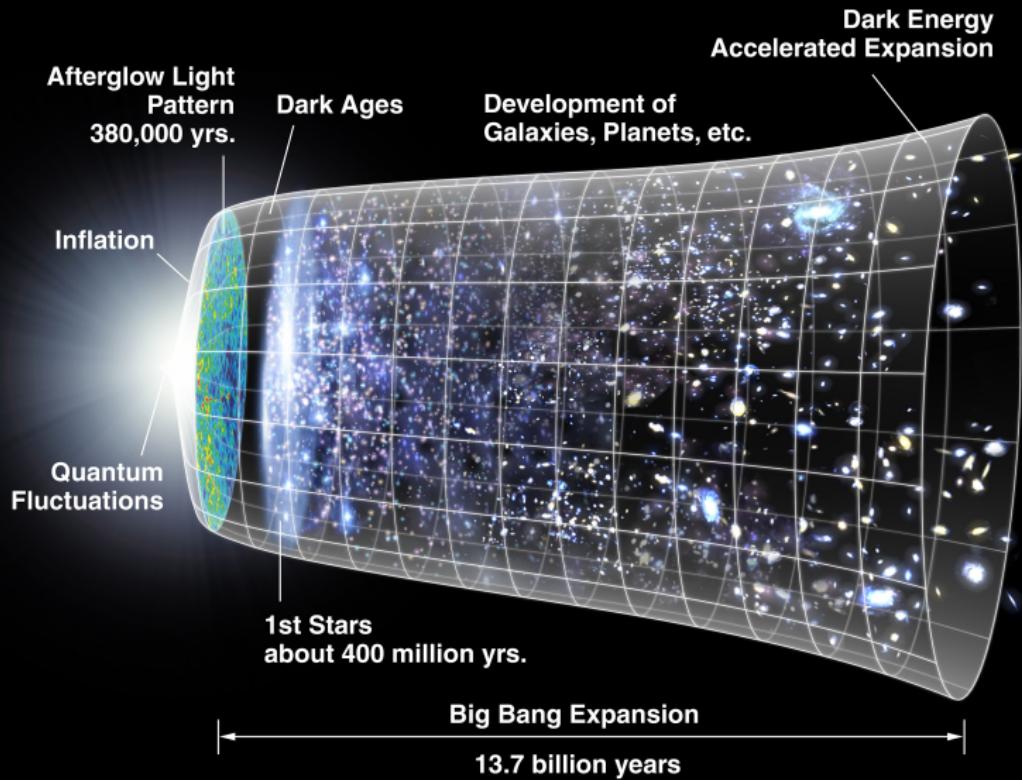


(Credit: Springel et al. 2005)

Baryon acoustic oscillations



(Source: BNL)



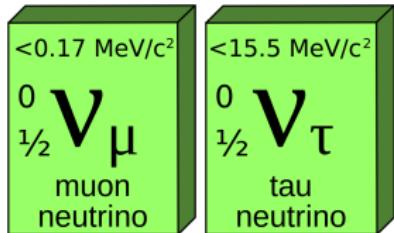
## Modified gravity



(Source: NASA)

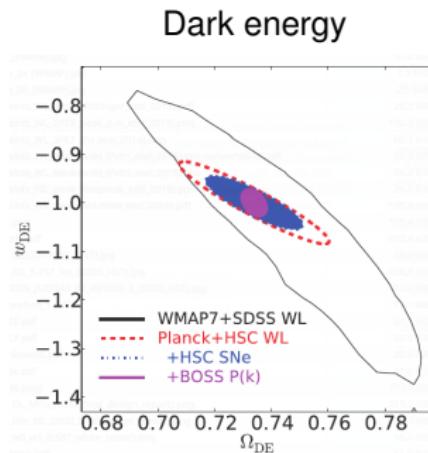
$$f(R) = -m^2 \frac{c_1(R/m^2)^n}{c_2(R/m^2)^n + 1}$$

## Massive neutrinos



(Source: MissMJ@Wikimedia/CC BY 3.0)

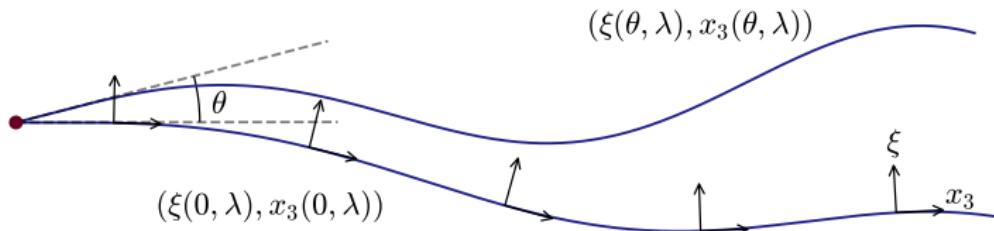
## WL as a probe beyond $\Lambda$ CDM



(HSC strategic survey proposal)

## **Theoretical basis**

## Geodesic deviation equation



Affine parameter  $\lambda$

2D angular position  $\theta$

2D transverse vector  $\xi = (x_1, x_2)$

Optical tidal matrix  $\mathcal{T}$

$$\frac{d^2 \xi(\theta, \lambda)}{d\lambda^2} = \mathcal{T}(x_1, x_2, x_3) \xi(\theta, \lambda)$$

$\mathcal{T}$  can be related to the gravitational potential  $\phi$

## Lensing potential

Gravitational potential  $\phi$

Lensing potential  $\psi$

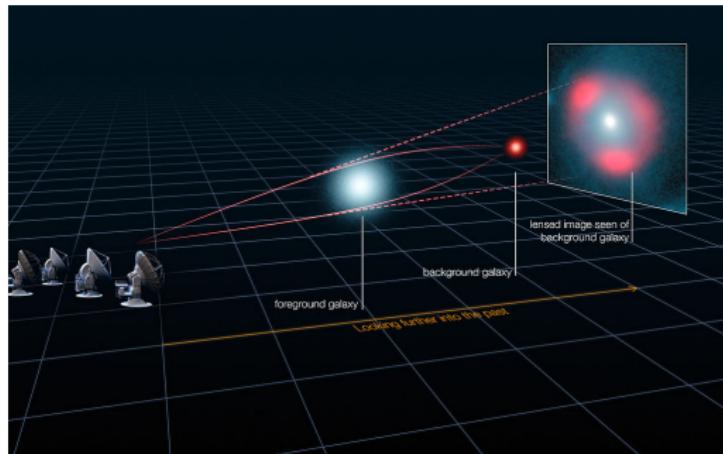
Comoving distances  $w, f_K(w)$

$$\psi(\boldsymbol{\theta}) \equiv \frac{2}{c^2} \int_0^w dw' \frac{f_K(w-w')}{f_K(w)f_K(w')} \phi(f_K(w')\boldsymbol{\theta}, w')$$

First-order distortion:

$$\mathcal{A}_{ij}(\boldsymbol{\theta}) = \delta_{ij} - \partial_i \partial_j \psi(\boldsymbol{\theta})$$

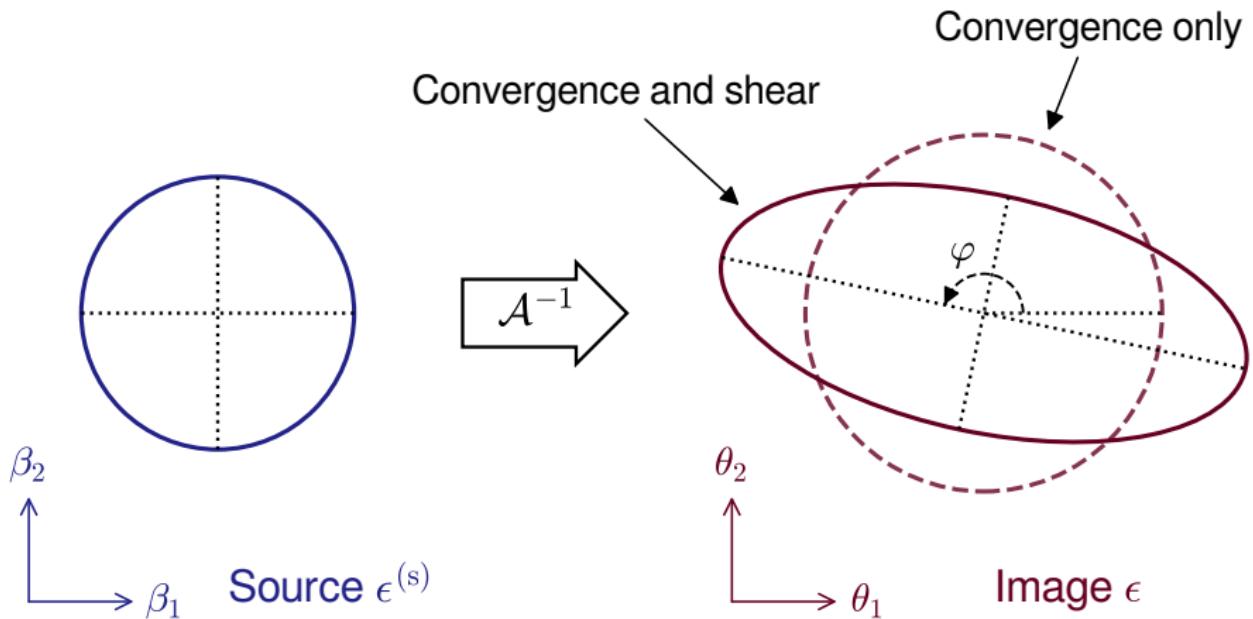
## Lensing potential



$$\psi(\boldsymbol{\theta}) \equiv \frac{2}{c^2} \int_0^w dw' \frac{f_K(w-w')}{f_K(w)f_K(w')} \phi(f_K(w')\boldsymbol{\theta}, w')$$

$$\mathcal{A}(\theta) = \begin{pmatrix} 1 - \kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1 - \kappa + \gamma_1 \end{pmatrix}$$

$\kappa$  — convergence — “projected mass”  
 $\gamma = \gamma_1 + i\gamma_2$  — shear — distortion



## Projected mass

Matter density contrast  $\delta$

Scale factor  $a$

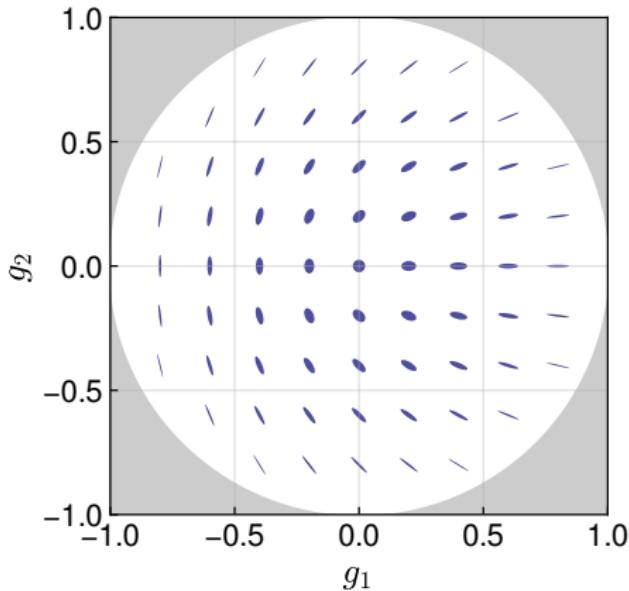
Comoving distances  $w, f_K(w)$

Various constants  $c, H_0, \Omega_m$

$$\kappa(\boldsymbol{\theta}, w) = \frac{3H_0^2\Omega_m}{2c^2} \int_0^w dw' \frac{f_K(w-w')f_K(w')}{f_K(w)} \frac{\delta(f_K(w')\boldsymbol{\theta}, w')}{a(w')}$$

$\kappa$  is a distance-weighted projection of  $\delta$

## Shape and shear



Intrinsic ellipticity  $\epsilon^{(s)}$   
as a random variable

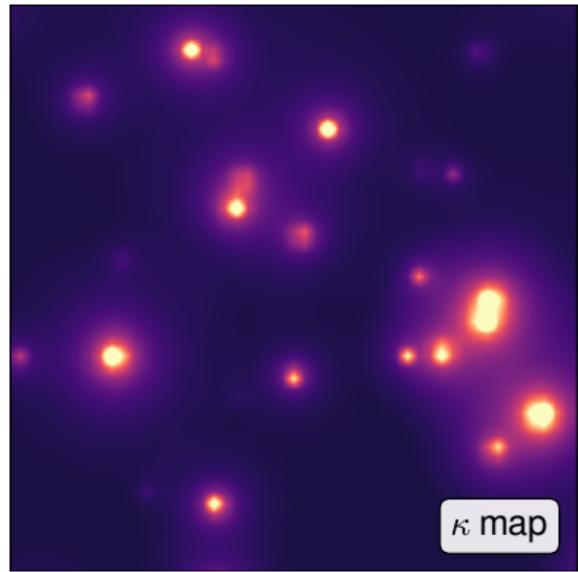
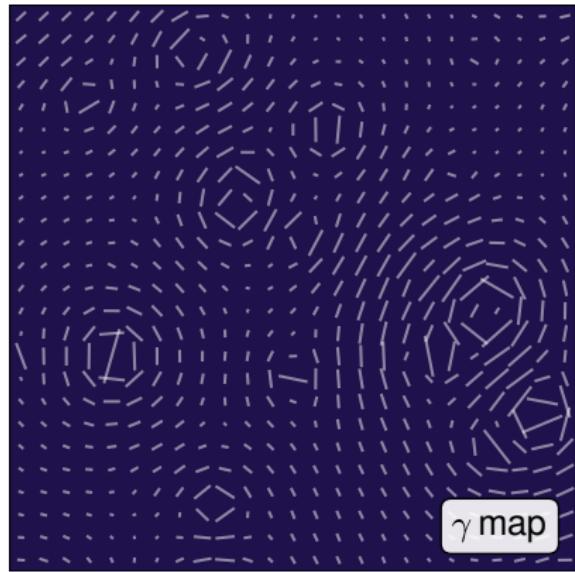
The observed one is  
 $\epsilon \approx \epsilon^{(s)} + g$

where  $g \equiv \frac{\gamma}{1 - \kappa} \approx \gamma$

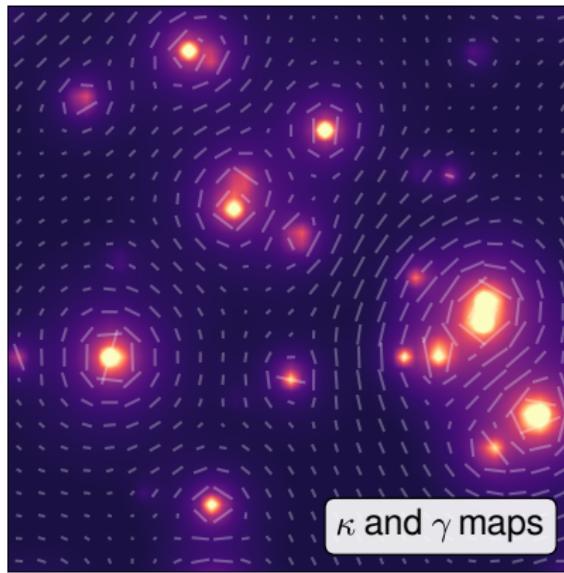
$$\sigma_{\epsilon^{(s)}} \approx 0.4$$

$|\gamma| \sim \text{few percents}$

$\kappa$  and  $\gamma$  are related quantities

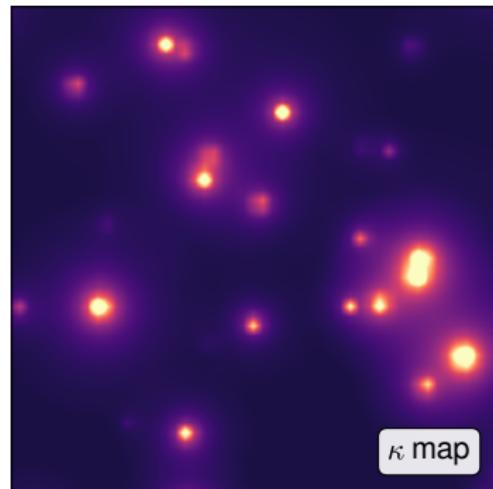
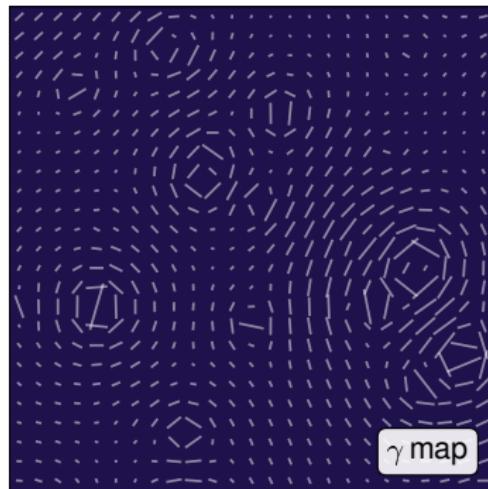


$\kappa$  and  $\gamma$  are related quantities



What to measure? Dark energy  
How to measure?

Wake up if you fall asleep



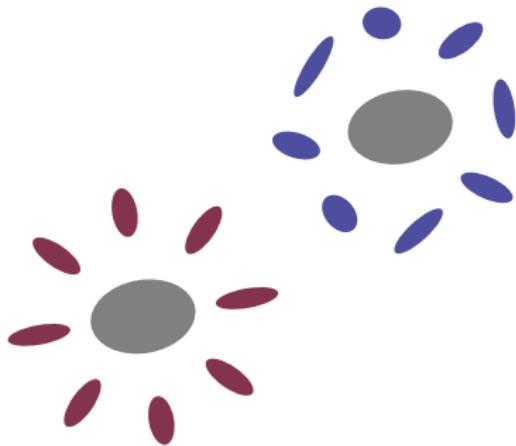
Stretch of galaxy images  
induced by gravitation

Underlying structures predicted  
by cosmological models

## **Modelling & observational challenges**

## Intrinsic alignment

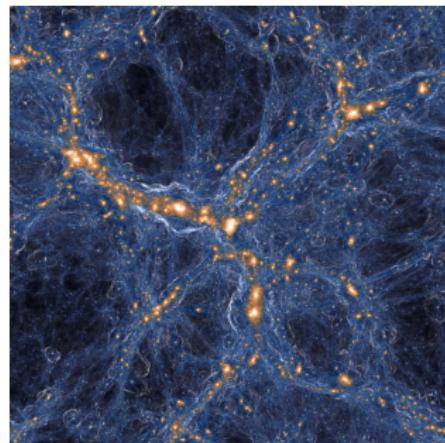
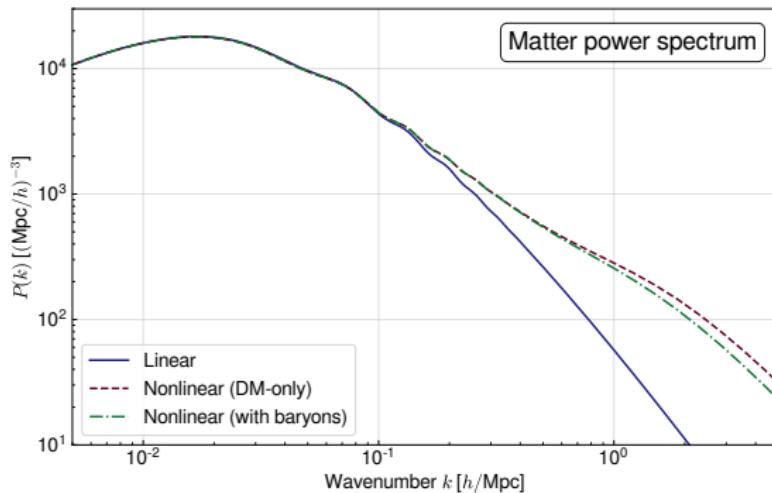
Random orientation



Intrinsic alignment

- IA mimics lensing signals
- Models exist
- Are they accurate enough?

## Baryonic effects

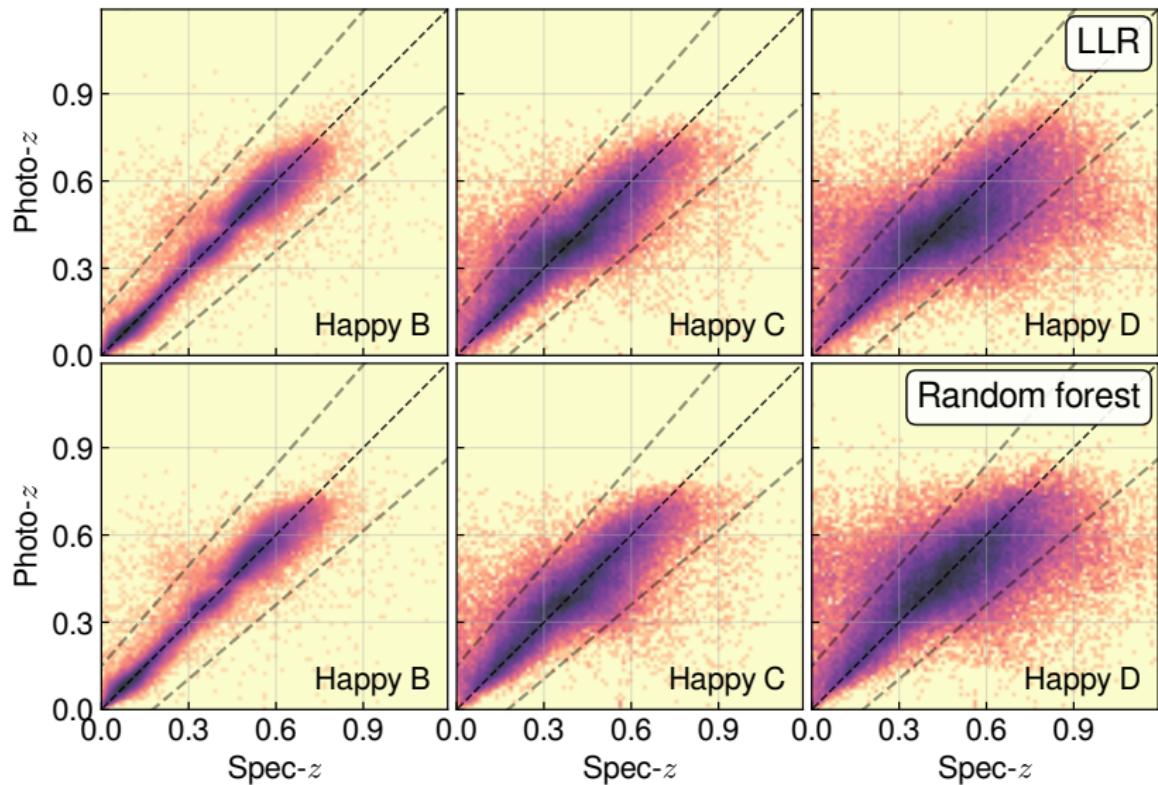


(Source: TNG Collaboration)

- Baryons contribute to lensing (of course!)
- Difficult to model
- We want to control the power spectrum at 2%
- Can cut scales, but will also lose data :(

Beck, Lin, et al. (2017)

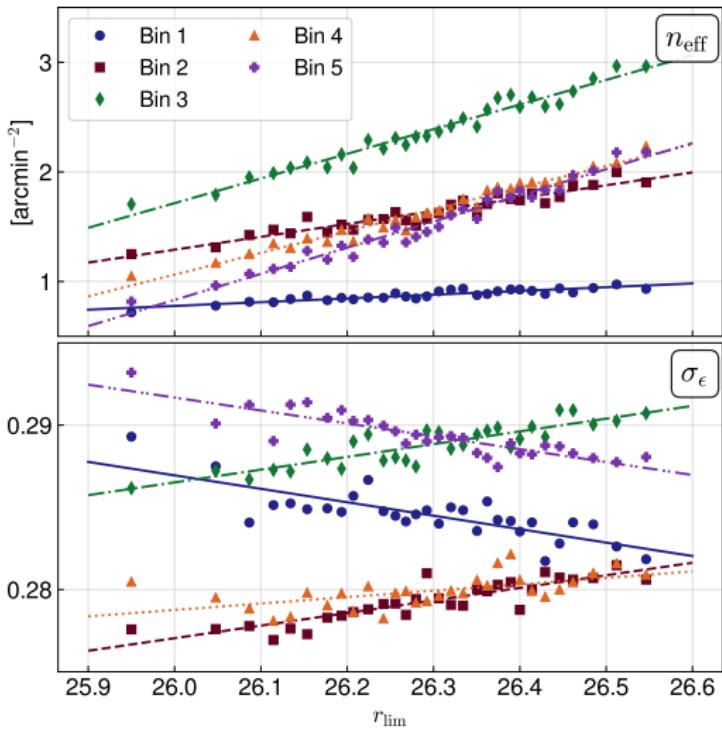
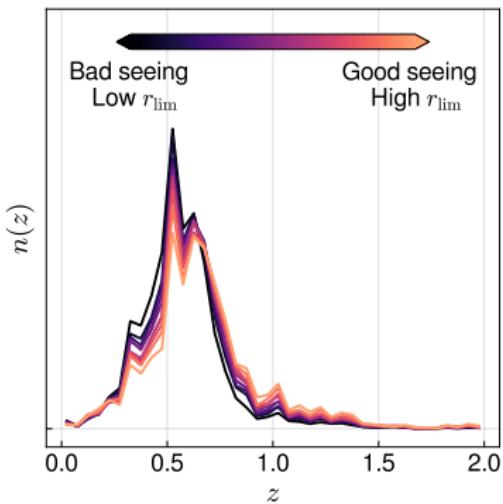
## Photometric redshift errors



Joachimi, Lin, et al. in prep.

## Variable depth effect

Redshift distributions  $n(z)$ ,  
source density  $n_{\text{eff}}$ ,  
and shape noise  $\sigma_{\epsilon}$   
vary with  $r$ -band  
magnitude limit  $r_{\text{lim}}$ .



NGC 201 by ESA/Hubble

## Galaxy shape in real life



Original galaxy



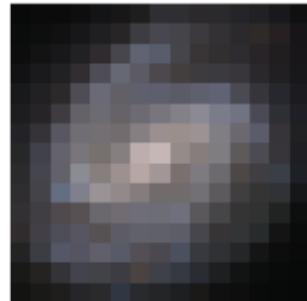
Instrumental noise



Lensing



PSF

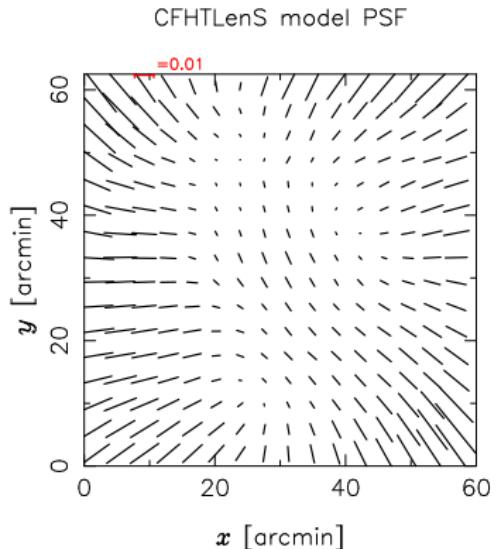


Pixelization

## Point spread function (PSF)

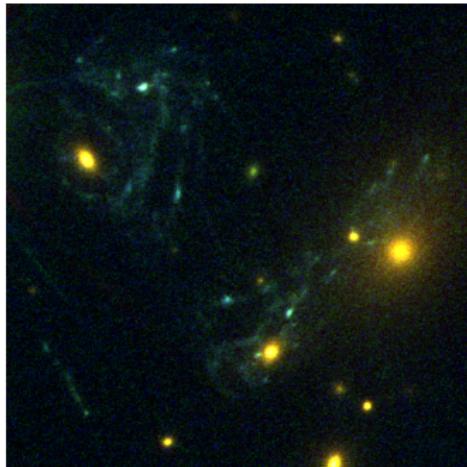


Shear: a percent-level effect  
PSF: sub- to few percents



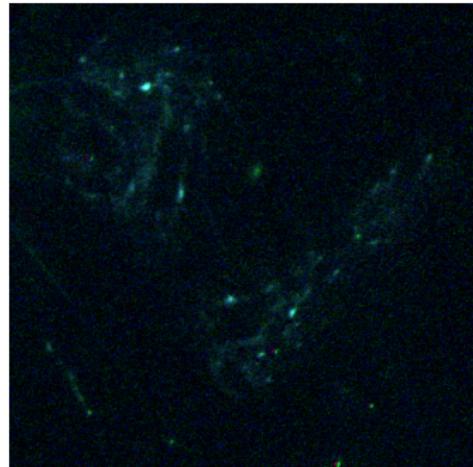
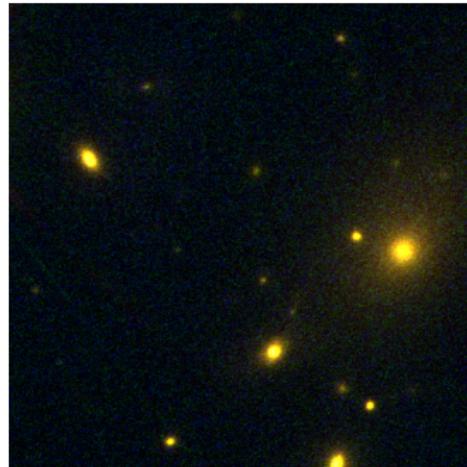
(van Uitert & Schneider 2016)

With state-of-the-art techniques, calibration of residuals is still needed

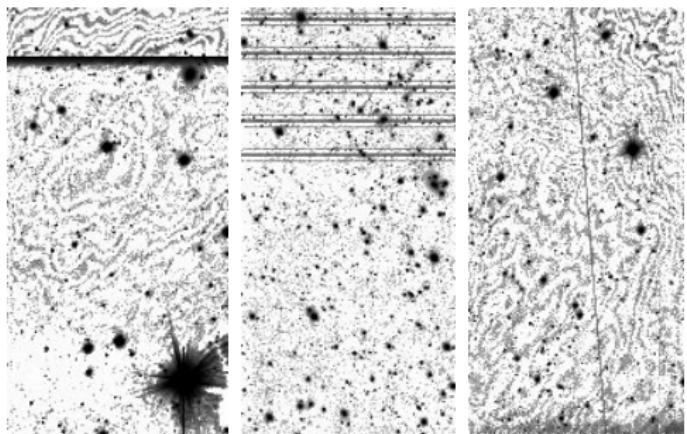
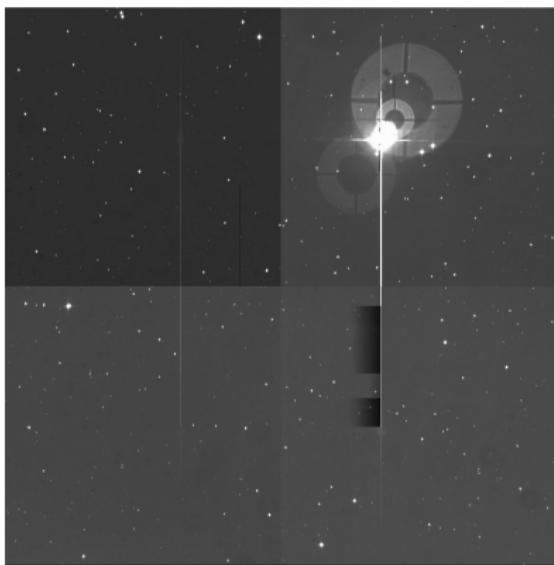


Galaxy blending

Joseph et al. (2016)



## CCD defects

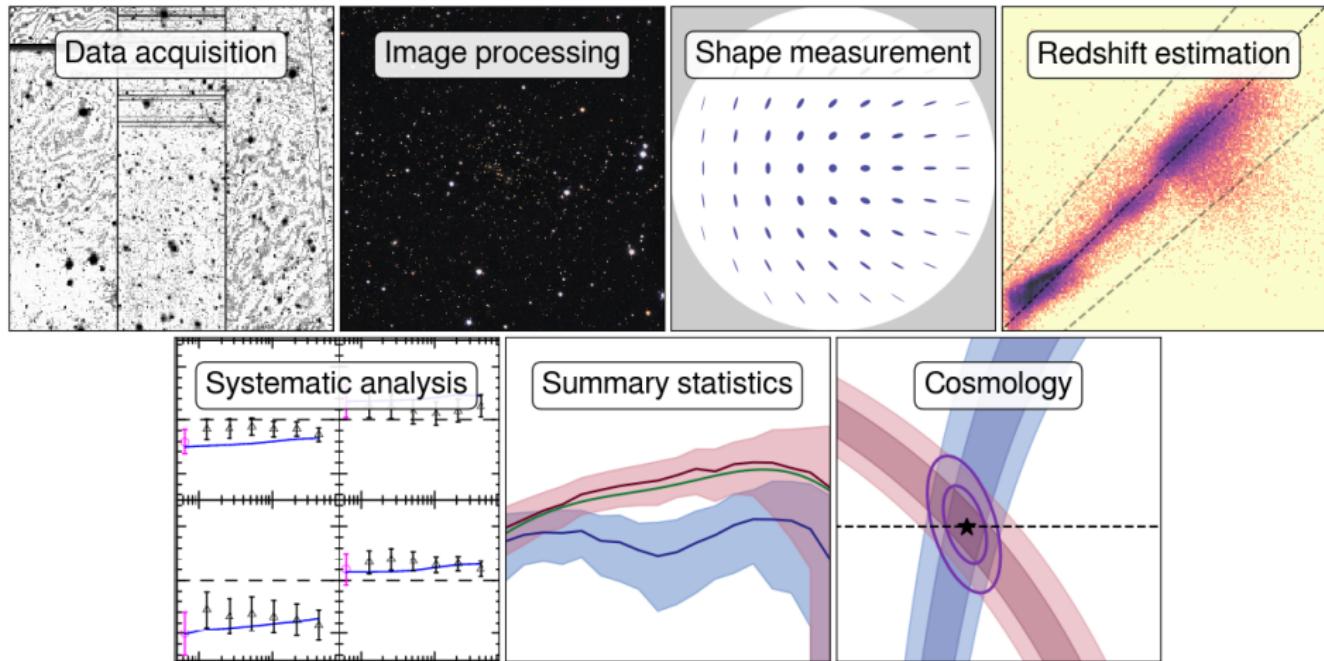


Source:

MDM Observatory  
Amon et al. (2018a)



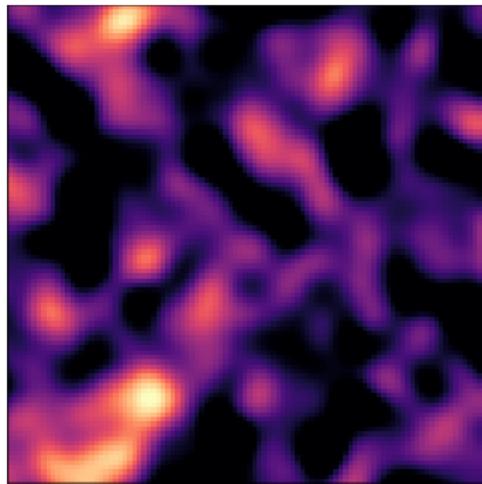
# Weak-lensing pipeline



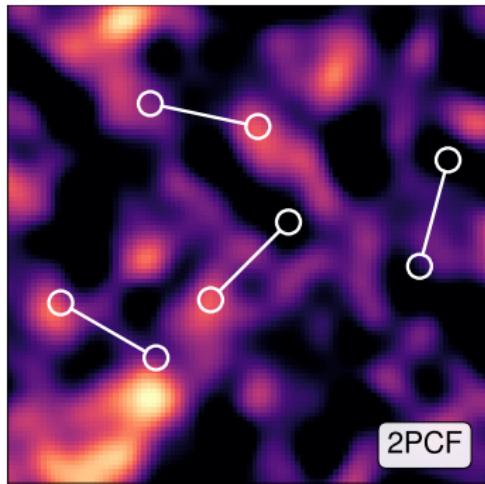
Amon et al. (2018a); Tudorica & KiDS; Beck, Lin, et al. (2017); Heymans et al. (2012)

**State of the art**

## How to extract cosmological information?



## How to extract cosmological information?



Two-point correlation functions:

$$\xi_{\pm}(\theta) \equiv \langle \gamma_+ \gamma_+ \rangle(\theta) \pm \langle \gamma_{\times} \gamma_{\times} \rangle(\theta)$$

$$\xi_+(\theta) = \int_0^{+\infty} \frac{\ell d\ell}{2\pi} J_0(\ell\theta) P_\kappa(\ell)$$

$$\xi_-(\theta) = \int_0^{+\infty} \frac{\ell d\ell}{2\pi} J_4(\ell\theta) P_\kappa(\ell)$$

# KiDS



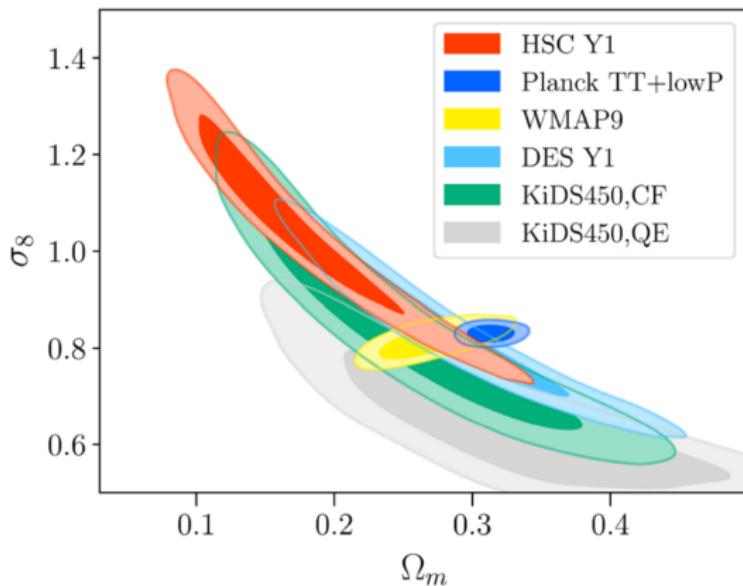
Benchmark surveys



	KiDS	DES	HSC
Effective Area [deg <sup>2</sup> ]	360	1321	137
Magnitude limits*	24.9	24	26.4
Effective galaxy density [arcmin <sup>-2</sup> ]	8.5	5.5	16.5

\*Respectively for  $i'$ -,  $r$ -,  $i$ -, and  $i$ -bands

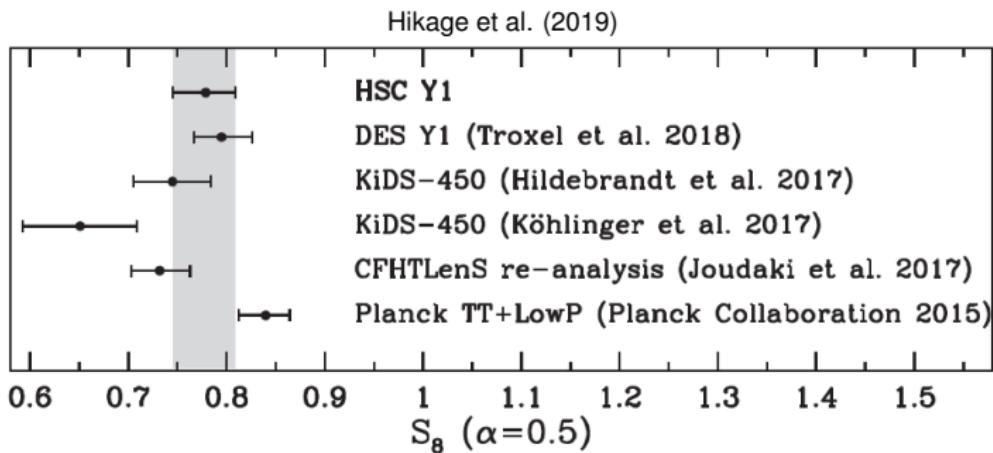
## Cosmological constraints



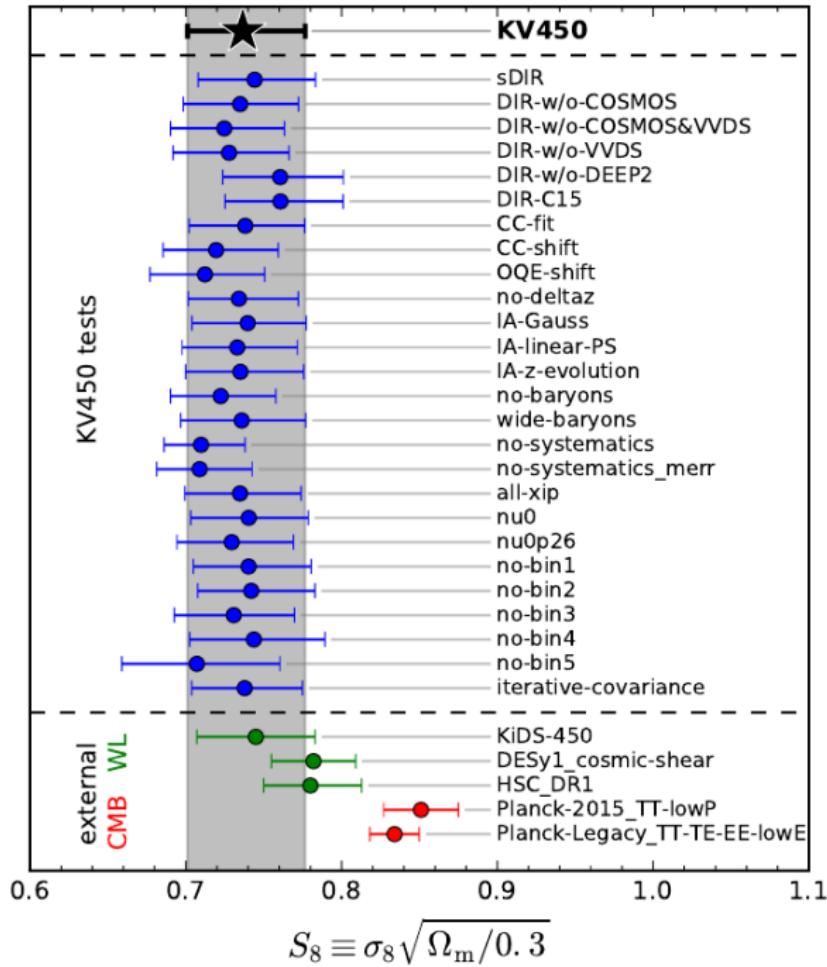
$\Omega_m$  = matter abundance  
 $\sigma_8$  = matter fluctuation

Hildebrandt et al. (2017)  
Troxel et al. (2018)  
Hikage et al. (2019)

## Cosmological constraints



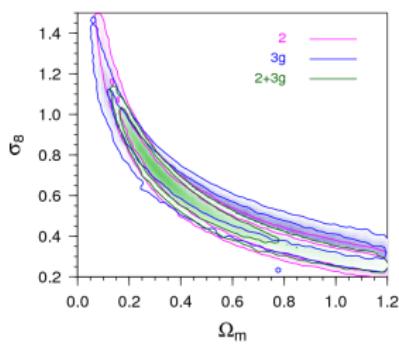
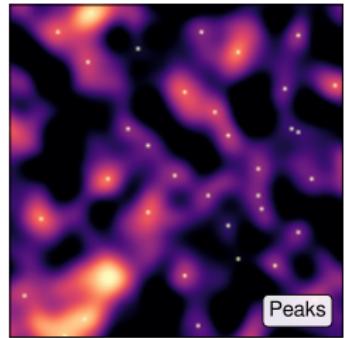
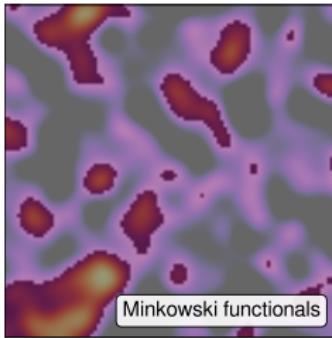
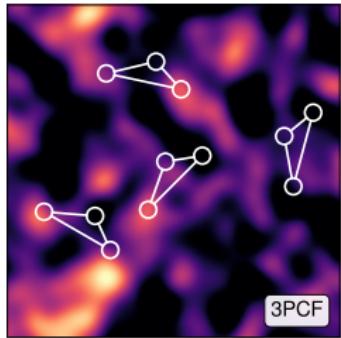
$$S_8 = \sigma_8(\Omega_m/0.3)^\alpha$$



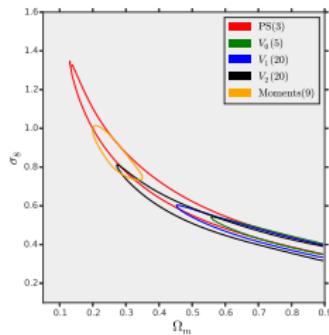
Systematic tests  
from WL

Hildebrandt et al. (2019)

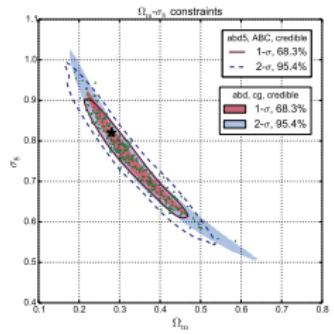
# Non-Gaussian estimators



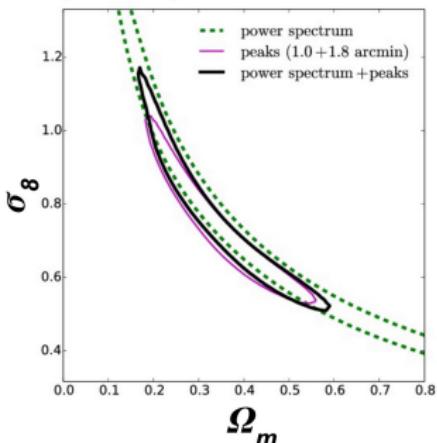
Fu et al. (2014)



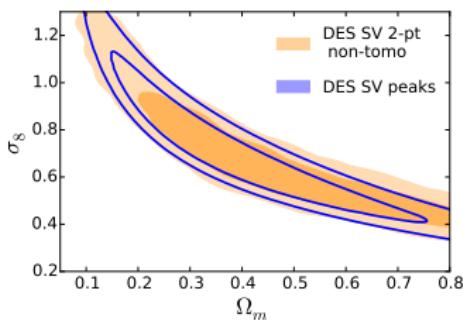
Petri et al. (2015)



Lin & Kilbinger (2015b)

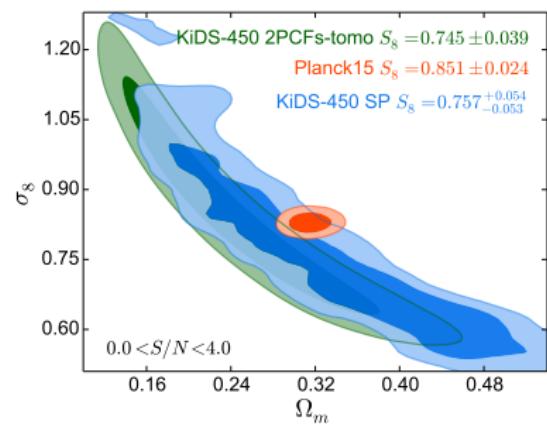


Liu et al. (2015)



Kacprzak et al. (2016)

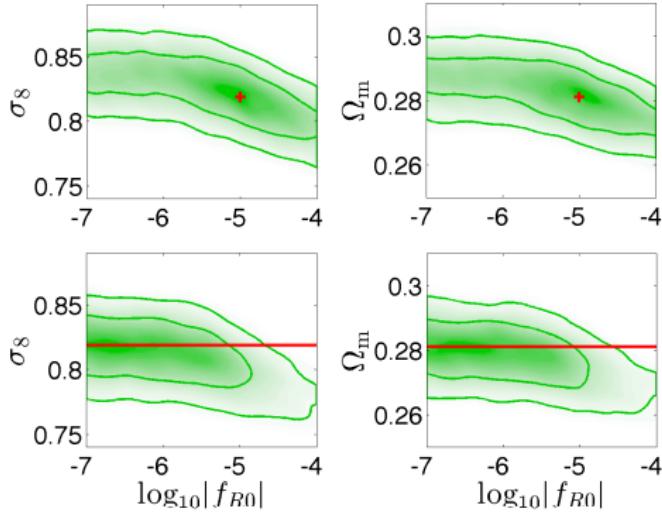
## Results from lensing peaks



Martinet et al. (2018)

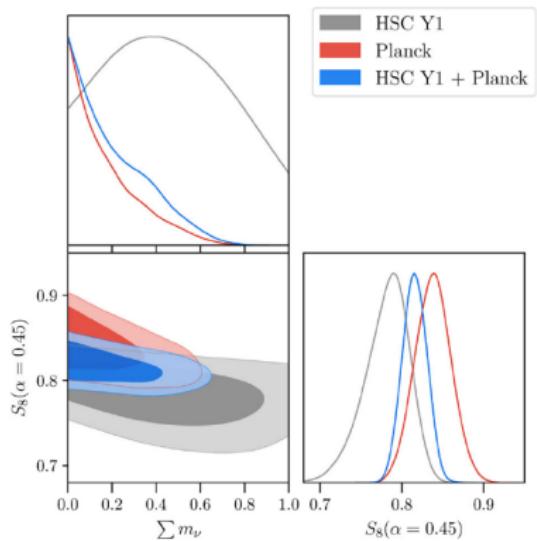
# Constraints on extended physics

Modified gravity



Liu et al. (2016)

Massive neutrinos



Hikage et al. (2019)

## Future perspectives

## Ongoing surveys keep collecting data



Kilo-Degree Survey     $360 \Rightarrow 770 \Rightarrow 1000 \text{ deg}^2$



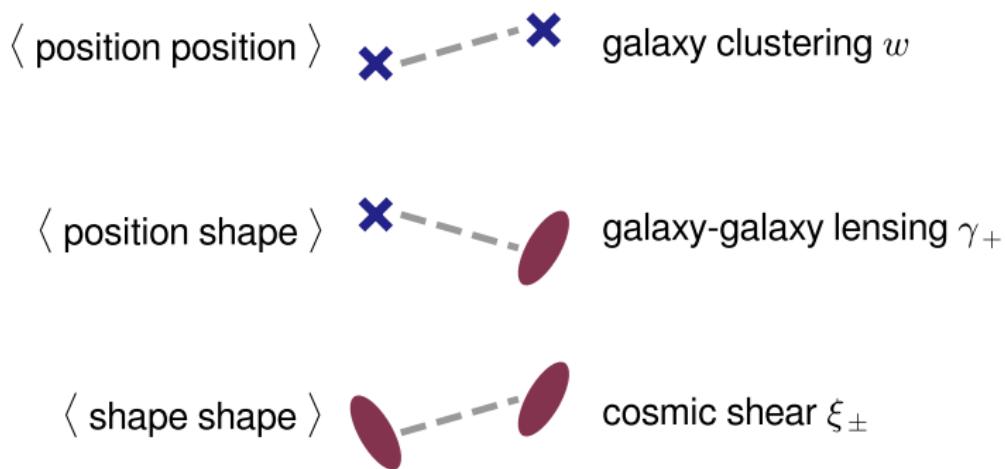
$1321 \Rightarrow \dots \Rightarrow 6000 \text{ deg}^2$



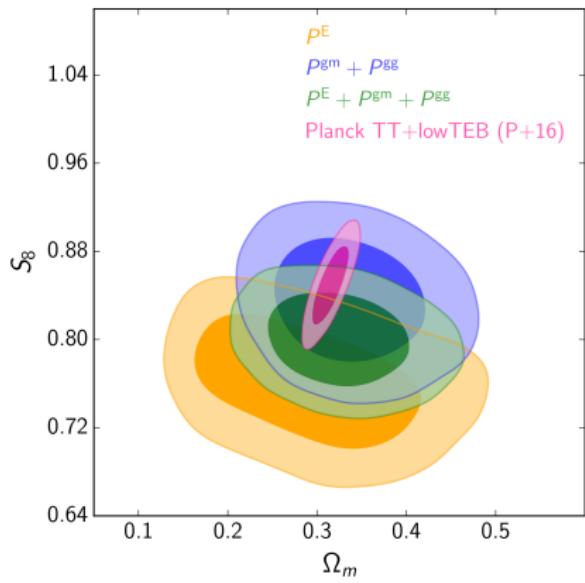
Hyper Suprime-Cam     $130 \Rightarrow \dots \Rightarrow 1000 \text{ deg}^2$

3×2pt analysis

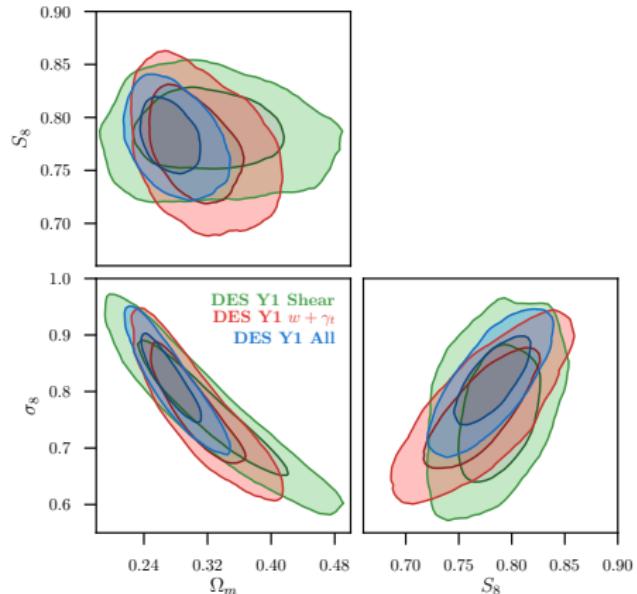
- Galaxy position: biased tracer of matter
- Galaxy shape: noisy tracer of projected matter



## 3×2pt: better constraints



KiDS Collaboration  
(van Uitert et al. 2018)



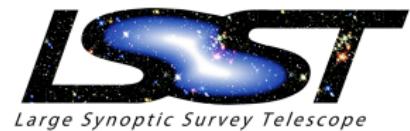
DES Collaboration (2018)



- Space mission at L2 point
- 1.2 meter entrance pupil & 609 Mpixel camera
- 3 infrared photometry bands: YJH
- Area =  $15000 \text{ deg}^2$
- Visible band limit = 24.5



Euclid\_NISP@Twitter

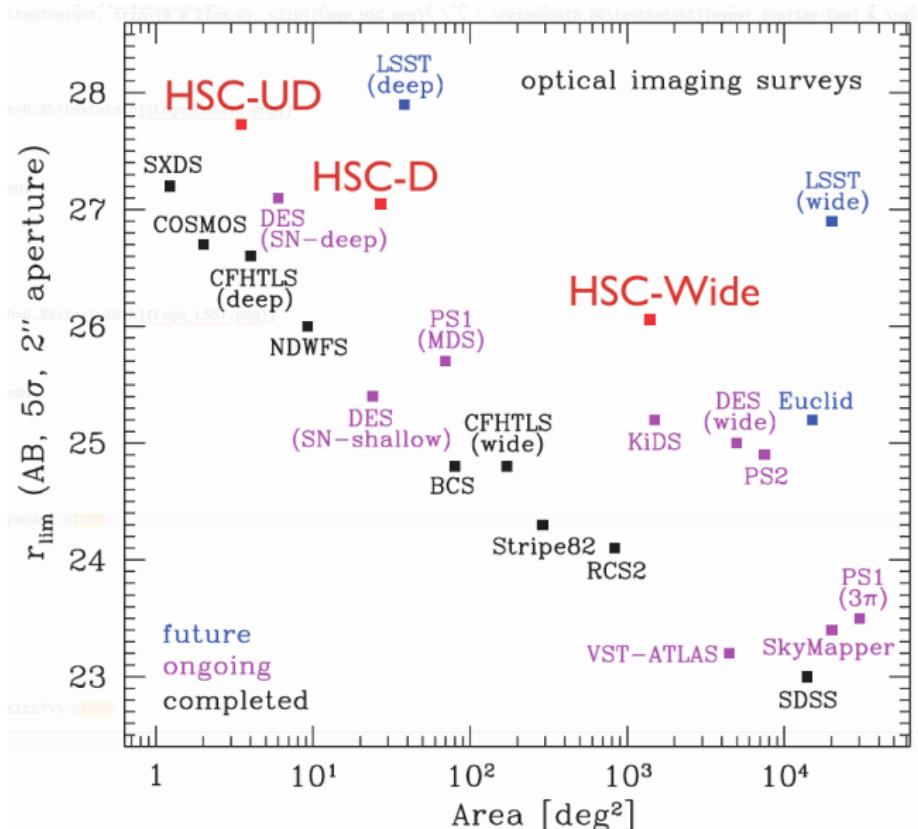


- Located at the sommet of Cerro Pachón in Chile
- 8.4 meter mirror & 3.2 Gpixel camera
- 6 photometry bands: ugrizy
- Area =  $20000 \text{ deg}^2$
- $i$ -band limit = 27.0

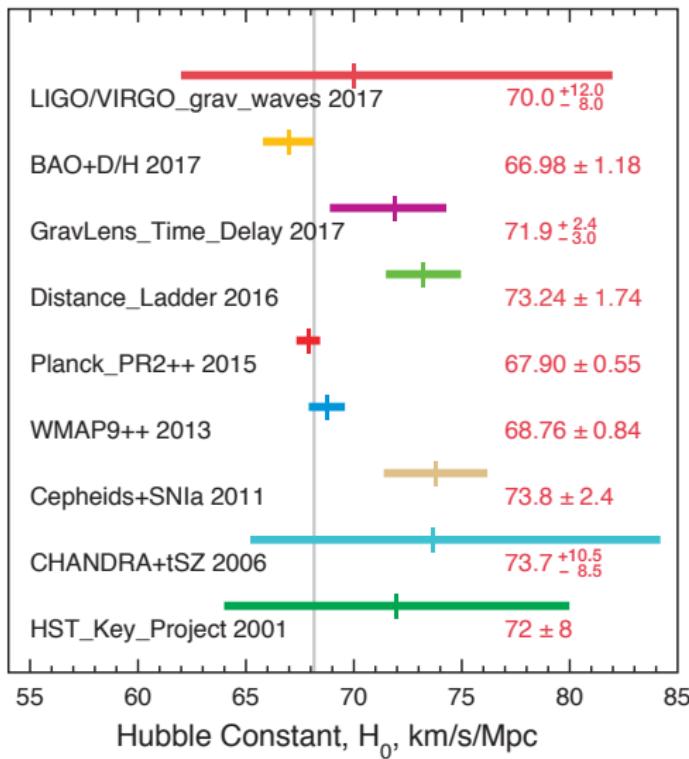


LSST@Twitter

# Optical depth vs survey area

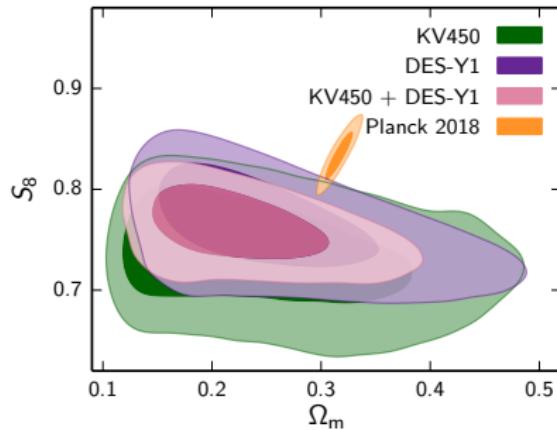


## Tensions: systematics or new physics?



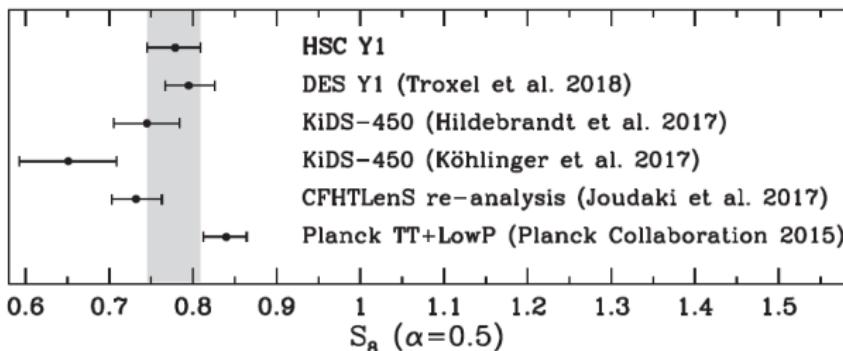
Source: NASA

# Tensions: systematics or new physics?

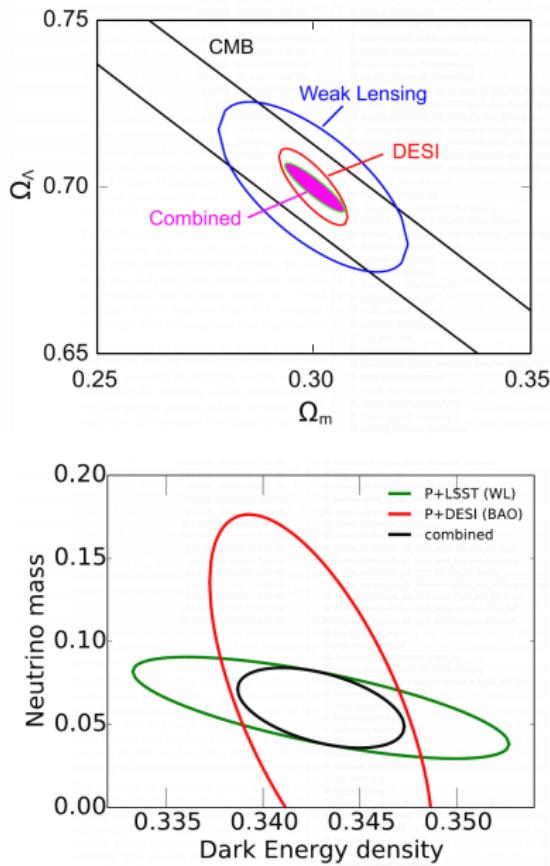


Joudaki et al. submitted

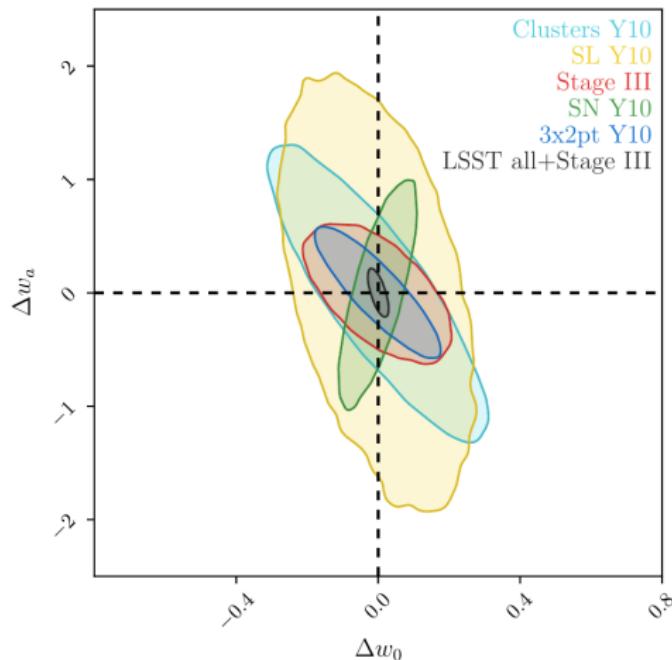
Hikage et al. (2019)



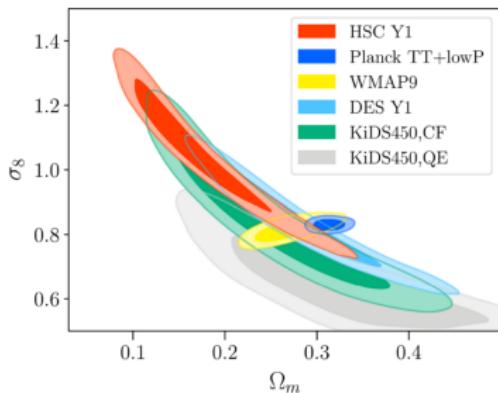
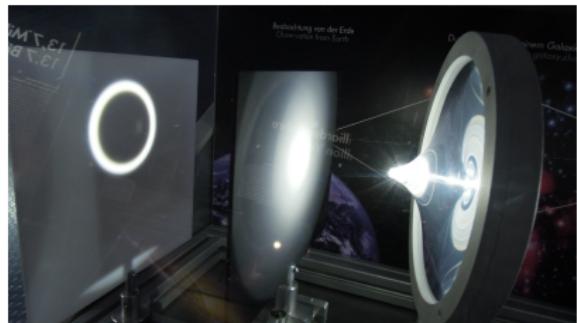
# Synergy



Source:  
LSST science requirements document  
DESI final design report



- What to measure?
- How to measure?
- What do we really measure?
- What have been measured?
- What will be measured?



- Dark energy
- From late-time evolution of cosmic structures
- Tiny distortions of galaxy images
- Some bananas
- Tiny bananas/potatoes or new discoveries!

# Backup slides

## Impact from variable depth

